ENSO Bred Vectors in Coupled Ocean-Atmosphere General Circulation Models

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ABSTRACT

The breeding method has been implemented in the NASA Seasonal-to-Interannual Prediction Project (NSIPP) coupled general circulation model (CGCM) with the ultimate goal of improving operational seasonal to interannual climate predictions through ensemble forecasting and data assimilation. This is the first attempt to isolate the evolving ENSO instability and its corresponding global atmospheric response in a fully coupled ocean–atmosphere GCM. The results herein show that the growth rate of the coupled bred vectors (BVs) is sensitive to the ENSO phases of the evolving background flow and peaks about 3 months before an ENSO event. The structure of the dominant growing BV modes also evolves with the background ENSO and exhibits a larger amplitude in the eastern tropical Pacific, reflecting the natural dynamical sensitivity associated with the shallow thermocline at the eastern boundary. The key features of coupled bred vectors of the NSIPP CGCM are reproduced when using the NCEP CGCM, an independently developed coupled general circulation model.

1. Introduction

The El Niño-Southern Oscillation (ENSO) phenomenon is responsible for a large portion of interannual variability in the tropical Pacific. ENSO also has a global impact in climate anomalies and extreme weather events. Feedbacks through atmosphere-ocean coupling in the Tropics characterize the covariability of wind, SST, and thermocline (or warm water volume) of ENSO. Many features of the ENSO events have been explained by the delayed oscillator mechanism owing to propagating downwelling/upwelling information in the upper ocean associated with equatorial waves (Schopf and Suarez 1988; Suarez and Schopf 1988; Battisti 1988). Jin (1997) further emphasized the importance of the variations of warm water volume in the upper ocean with a warm water recharge/discharge mechanism. It has been shown that the coupled dynamic/thermodynamic mechanisms, that is, the thermocline and Ekman feedbacks, responsible for delayed or recharge/discharge

oscillators, can explain both the west–east asymmetry in the climate mean state and the ENSO variability in the equatorial Pacific basin (Cai 1995; Jin 1996; Dijkstra and Neelin 1999; Van der Vaart et al. 2000; Cai 2003). The dynamical atmosphere–ocean coupled models constructed with the concept of the delayed or recharge/ discharge oscillator have shown valuable prediction skill for the ENSO events (Cane et al. 1986; Zebiak and Cane 1987). The strong weather and climate impact from ENSO has motivated the advancement of prediction tools from simple anomaly coupled models to fully coupled global ocean–atmosphere general circulation models (CGCMs).

Factors that influence the skill in forecasting seasonal-interannual SST anomalies include the errors in oceanic and atmospheric initial conditions, atmospheric stochastic variability, and model errors. It is known that the presence of errors in the initial condition limits the ENSO prediction skill (Latif et al. 1998) and that an ensemble forecast should sample the uncertainties in the initial condition (Stockdale et al. 1998). Vialard et al. (2003) performed a series of ensemble forecast experiments with a state-of-the-art coupled GCM using wind and SST perturbations and stochastic physics, individually or combining all of them. Their results sug-

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gest that the uncertainties in SST determine the spread of ensemble forecasts in early months of the forecast, while perturbations of the wind stress or atmospheric internal variability are less efficient in generating SST variations. These results are supported by Chen et al. (2004) who argue that the evolution of El Niño is controlled to a large degree by self-sustaining internal dynamics in the Tropics. These results suggest that the ENSO prediction depends more on initial conditions than on unpredictable atmospheric noise and that there is a good reason to investigate the inclusion of coupled initial perturbations for ensemble ENSO prediction.

In the ENSO ensemble prediction, the challenge is how to generate ensemble perturbations that can effectively represent SST uncertainties in seasonal-interannual scale in a CGCM. Moreover, initial ensemble perturbations need to be constructed in a coupled manner in order to ensure that they reflect the uncertainties associated with the coupled instability. In addition, ensemble perturbations for ENSO prediction should also reflect the uncertainties in teleconnected atmospheric variables to improve coupled forecast skill beyond the tropical Pacific region.

Methods for generating ensemble perturbations can be loosely categorized into linear and nonlinear approaches. The singular vector linear approach looks for the optimal initial perturbations that will maximize the growth of the perturbations after a chosen period with a chosen norm. With an optimization time of 3-6 months and the choice of the SST norm, Penland and Sardeshmukh (1995), Chen et al. (1997), and Thompson (1998) showed that a final singular vector with large amplitude of the SST signal is located in the southeastern Pacific. It should be pointed out that, even though the growth rate of their singular vector strongly depends on seasonal cycle and ENSO phase, their initial singular vectors are insensitive to both. However, also using a SST norm, Xue et al. (1994, 1997a,b) and Fan et al. (2000) obtained ENSO-like initial singular vectors, emphasizing that the signals in the eastern Pacific are more concentrated toward the equator, even though their final singular vectors are very similar to those found in Chen et al. (1997) and Thompson (1998). Finally, a very different pattern compared to all of the other studies has been obtained from a series of studies done by Moore and Kleeman (1996, 1997, 1999a,b, 2001). Their results emphasize large signals in the west to central Pacific. When considering a multivariable perturbation norm, Fan et al. (2000) and Moore and Kleeman (2001) reached different conclusions on the relative importance between the SST and the thermocline. The strong dependence on the choice of norm and the models may be of concern in drawing a robust conclusion as to their use for ENSO ensemble perturbations. Moreover, with a very complex system like a CGCM that includes a wide range of instabilities, leading singular vectors would be dominated by the fast growing error related to weather and even convection (Peña and Kalnay 2004). Thus, to obtain an ENSOrelated singular vector in a coupled GCM, one needs to exclude less relevant fast growing components explicitly from the tangent linear operator (Kleeman et al. 2003). The computational/development costs are also a limitation for the singular vector method since it requires constructing coupled tangent linear and adjoint operators.

The breeding method proposed by Toth and Kalnay (1993, 1997) is designed to estimate the shape of the growing dynamic error using the full nonlinear model. This method takes advantage of the early nonlinear saturation of convective instabilities compared to baroclinic instabilities. Toth and Kalnay (1996) suggested this advantage could be applied in a coupled oceanatmosphere system to isolate ENSO coupled instabilities from the faster weather-related instabilities. Cai et al. (2003) first tested the breeding method in a coupled system using the ZC model (Zebiak and Cane 1987). They found that the bred vector (BV) growth rate is weakest at the peak time of the ENSO states (both positive and negative) and strongest between the events. Also, the coupled bred vectors are insensitive to the choice of norm but very sensitive to the background ENSO phase and the annual cycle. It should be pointed out that the ZC model only has ENSO-related instability and the fast processes are already explicitly excluded from the ZC model. Peña and Kalnay (2004) illustrated the idea that breeding is able to isolate the slow modes of a coupled system when rescaling intervals and amplitudes are chosen from physically appropriate scales and the rescaling factor is obtained from the slow component of the system. Independent work by Boffetta et al. (1998) also demonstrated that choosing the perturbation size is a powerful tool to isolate the slow mode in a system with multiple time scales.

The results with the simple ZC model encouraged us to implement the breeding method in a CGCM, without sacrificing resolution or simplifying model physics. The new challenge is that a CGCM includes many types of instabilities with different time scales. Therefore, we need to demonstrate, as a first step, whether we can obtain the slowly growing coupled instabilities as in Cai et al. (2003) using breeding in a comprehensive CGCM. Our objective is to identify the characteristics of bred vectors associated with the ENSO derived from the CGCM and to investigate whether an ENSO-related coupled instability can be isolated from weather-related instabilities using the breeding method. Specifically, in this paper, we address the following questions. 1) Can breeding be used to identify or detect the coupled, slowly growing ENSO instability and isolate it from other short-term instabilities? 2) Is the coupled BV mode sensitive to the ENSO phases? and 3) Are the main characteristics of coupled bred vectors reproducible with different coupled ocean–atmosphere GCMs?

The paper is organized as follows. In section 2, we give a brief description of the National Aeronautics and Space Administration's (NASA's) Seasonal-to-Interannual Prediction Project (NSIPP) coupled model that has been used to generate coupled bred vectors. The simulated ENSO variability in the NSIPP model is also included in section 2. Section 3 describes how the breeding method is applied in a coupled GCM for isolating the slowly varying coupled instability. Section 4 describes the main characteristics of coupled bred vectors derived in the NSIPP model. A comparison of the results obtained from NSIPP and from the National Centers for Environmental Prediction Coupled Forecast System Model (NCEP/CFS03) is also presented in section 4. A brief summary and discussion of the next phase of our research are included in section 5.

2. Breeding method with the NSIPP coupled global circulation model

In this study, we implemented the breeding method on the NSIPP coupled ocean–atmosphere general circulation model. The NSIPP coupled model is a fully coupled global ocean–atmosphere–land system developed at the NASA Goddard Space Flight Center (GSFC) (Vintzileos et al. 2003). It comprises the NSIPP atmospheric model (AGCM) (Bacmeister and Suarez 2002; Bacmeister et al. 2000), the Poseidon ocean model (OGCM) (Schopf and Loughe 1995; Yang et al. 1999), and the Mosaic land surface model (LSM) (Koster and Suarez 1992). The official NSIPP Web site contains detailed information about the NSIPP coupled model (http://nsipp.gsfc.nasa.gov/).

A 62-yr simulation run had been made with a research version of the NSIPP CGCM with a resolution of 3° latitude by 3.75° longitude and 34 sigma layers in the AGCM and $\frac{1}{2}^{\circ}$ latitude by 1.25° longitude and 27 layers in the OGCM. This integration constitutes our "nature run" and is referred to as the "background" in this paper. The bred perturbations are grown upon the evolving background flow. The wind stress, SST, and thermocline anomalies from this long simulation exhibit coupled ENSO interannual variability. However, the ENSO cycle of the control run has an unrealistically strong biennial component rather than the observed dominant 3–7-yr period. In addition, the standard deamplitude



FIG. 1. Schematic showing that, if the rescaling time interval for breeding is larger than t_0 , the saturation time of the fast noise, and smaller than the time t_1 , when nonlinearities reduce the growth of the slow signal, the relative amplitude of the linearly growing slow signal is boosted with respect to the noise.

viation of the SST anomaly in the eastern Pacific is only half of the observed. This problem has been attributed to the atmospheric longitudinal circulation near the equator (Rienecker et al. 2000). The spatial patterns of the coupled ENSO variability of the background are shown in the left panels of Figs. 4–6 and will be discussed together with the bred vector spatial structure in section 3.

We used a 10-yr model simulation run to perform breeding experiments under a "perfect model scenario," that is, assuming that the unperturbed simulation run is the "truth" (or analysis in a forecast system). The breeding method (Toth and Kalnay 1993, 1996, 1997) was originally developed to "breed" growing modes related to synoptic baroclinic instability for short-to-medium range atmospheric ensemble forecasting by taking advantage of the fact that small amplitude, but faster growing, convective instabilities saturate earlier. The idea that different amplitudes and time scales characterize different types of instabilities is applied to isolate the slowly growing coupled ENSO instability from the fast growing weather signal (see schematic Fig. 1). This is difficult to do using atmospheric variables since the amplitude of the weather noise is larger than that of the ENSO-related coupled signal. The slow, coupled perturbation can only be isolated by measuring the growing perturbations using the slowly evolving component of the coupled system, namely the ocean. Similarly, a physically meaningful choice of rescaling the period longer than two weeks is important in order to estimate the slowly varying coupled instability and saturate the growth of the weather signal (Peña and Kalnay 2004).

The procedure of breeding cycles in a coupled system has been described in Cai et al. (2003). Bred vectors are the periodically rescaled difference between the perturbed run and the nonperturbed run (background). The rescaling period (longer than two weeks) is chosen to allow fast weather instabilities to saturate well before the rescaling time, whereas the slowly evolving ENSO instability is still growing (Fig. 1). Both oceanic and atmospheric perturbations are scaled down with the same factor, measured by the growth of the ocean component. This gives a relative advantage to the slowly growing ENSO mode (as well as to any other slow instability present in the coupled system). In the next breeding cycle, the saturated fast instability perturbation starts with an unfavorable shape and does not have much room to grow, but the slow ENSO instability starts from a favorable (linear) shape that can still grow and evolve. Therefore, by repeating the breeding procedure (periodically resizing the perturbation and adding it to the background) we can enhance the relative amplitude of the slow instability and allow the bred perturbation to align along favorable growing directions. Although this does not completely isolate the ENSO perturbation, it gives it a relative boost compared to faster growing perturbations that saturate (Fig. 1), but other instabilities with time scales longer than the weather instabilities will be also present in the BV. In the next section, we focus on the dynamic structure of the coupled bred vector associated with the evolution of the background, which is viewed as "nature" in a perfect model scenario, since in this study we are not concerned with model error.

The breeding method was implemented in the NSIPP CGCM with a 1-month rescaling period and using the rms difference in the Niño-3 SST within the tropical Pacific domain (15°S–15°N, 120°E–90°W) as the rescaling norm. The rescaling amplitude of the rms SST was chosen to be 0.085°C, or about 10% of the background SST variability. The 1-month rescaling period, which is much longer than the time scale of the atmospheric baroclinic instability, is also a convenient choice because in the NSIPP system users can access only monthly model output. According to the experience in Cai et al. (2003) with the ZC model, the structure of the bred vector is rather insensitive to either the choice of the rescaling period (if it is long enough to saturate the weather signal) or the choice of the slow variable norm (L2 or the oceanic energy norm). Also, breeding experiments (M. Peña 2005, personal communication) with the NCEP coupled GCM using 15 days as the rescaling period have a similar behavior of the BV growth rate as with a 1-month rescaling period. The rescaling norm must be associated with the ocean component in order to capture the slowly growing instability. Since the SST directly represents the strength of the ENSO variability, it is natural to use it to detect the growing coupled instability. Because the research version of the NSIPP coupled GCM used in this paper is no longer available, it was not possible to test different breeding rescaling norms. However, tests with the operational version of the NSIPP coupled GCM show that the BV structure obtained is robust when using either a SST norm measured in the Niño-3 region or a thermocline norm measured in the tropical Pacific.

Two independent breeding runs were made starting from two perturbations created by taking the difference between two model states at randomly chosen months. Each run contains 123 months, starting from September of the 19th year to December of the 29th year of the 62-yr simulation run. The starting month is chosen to be well separated from the first major warming event, which takes place about 2 years into the breeding run. This is to ensure that the breeding experiment does not start when the background is dominated by the mature ENSO condition. Two independently generated breeding experiments show that bred vectors start to have similar structure after three months. Thus, we treat the first three months as a transient period allowing the bred vectors to align along the dynamics-dominated instability. The analysis presented below is derived from the remaining 120 breeding cycles (120 months). We found that two independent 10-yr breeding cycles yielded very similar bred vectors (not shown), so we combine the two bred vector perturbations as a single time series of 20 years to reduce sampling errors. Hereafter, we refer to the combined bred vectors as BV perturbations.

3. Results

a. Growth rate of coupled bred vectors

Bred vectors represent, by construction, the instabilities that have been growing in the recent past upon the background flow. In addition to ENSO, our method captures any instability with a time scale longer than 2 weeks. An example of such instability is shown in Fig. 2, a snapshot of the bred vector SST field (contours) together with the corresponding background SST field (shading) on 1 July of model year 24. It shows that the bred vector field has a large amplitude along the sharp zonal temperature gradient in the equatorial cold tongue, where tropical instability waves are present in the background along the edge of the cold tongue. The



FIG. 2. A snapshot of SST in the eastern Pacific showing the bred vectors' perturbation (contours: CI = 0.15° C) evolving with the background flow (shading with an interval of 1° C from 21° to 30° C) on 1 July of model year 24. The dotted contours of the BV indicate negative values.

bred perturbation is aligned with the background flow in such a way as to increase the amplitude of the waves. Tropical wave instability is active when the cold tongue is well established, like the fall season and the La Niña events, in both the background and the BV fields. The fact that the bred vector can capture the formation of tropical instability waves suggests BV sensitivity to the evolution of the background flow since the formation of such instability is strongly influenced by seasonal and interannual variability (Contreras 2002). We found that the BV structures related to the tropical instability waves disappear when the background is evolving toward a warm anomalous state. This example indicates that we can view the growth of the perturbations as a result of the superposition and competition among instabilities with different physical mechanisms and time scales. To analyze the ENSO component among all growth signals, we examine the relationship between the BV growth rate and the background ENSO variability, described by the Niño-3 index.

The growth rate of the coupled bred vectors is calculated based on the chosen rescaling norm of the perturbation field within the tropical Pacific region:

$$G(t) = \frac{\sqrt{\sum_{\text{NG}} \left[\text{BV}_{\text{SST}}(t)\right]^2}}{\sqrt{\sum_{\text{NG}} \left[\text{BV}_{\text{SST}}(t-1)\right]^2}},$$
(1)

where NG is the total number of model grid points in the Niño-3 region and t is the model time in months. In other words, we measure the growth rate of bred vectors by their amplification factor in the Niño-3 region within a month. In the 10-yr experiment, the mean of the bred vector growth rate is 3.8, and the standard deviation is 0.7. The mean growth rate is much higher than the result obtained from Cai et al. (2003), which has an ENSO growth rate ranging between 1 and 3. This is to be expected since the presence of additional instabilities in the coupled GCM contributes to the total growth of the perturbations, compared to the ZC model. For example, the tropical wave instability shown in Fig. 2 grows vigorously but with a shorter time scale than the ENSO variability.

To test whether there is a component of the perturbation growth (above the background noisy growth rate of about 3 per month) evolving upon the coupled ENSO background state (rather than growing randomly), we calculate the lag/lead correlation between the growth rate and the absolute value of the background Niño-3 index. We use the absolute value of the Niño-3 index in order to account for the large amplitude of both positive and negative SST anomalies. It is evident in Fig. 3 that the growth rate of coupled bred vectors tends to be largest about 3–4 months prior to the time when the background ENSO amplitude reaches its maximum stage (positive or negative).

Since the coupled GCM contains different types of instabilities, the correlation level of 0.22 in Fig. 3, although small, is significant in the context of the relative amplitude of the ENSO variability. To test statistical significance, we constructed the correlation between 1000 randomly generated time series and the absolute value of the background Niño-3 index. Each time series has the same mean and variance as the time series of the bred vector growth rates. Among the 1000 random samples, the mean correlation value is 0.017 and the standard deviation is 0.07. The accumulated percentage of the values of correlations indicates that the confi-



FIG. 3. Lead/lag correlations between the BV growth rate and the absolute value of the background Niño-3 index.

dence level is close to 99% in stating that a 0.2 correlation value represents a significant correlation to the background Niño-3 index. Therefore, the maximum in Fig. 3 supports the conclusion that the bred vector growth rate is related to and leads the background Niño-3 index.

In addition, the main growth signal takes place before the ENSO events in Fig. 3 because, by taking the absolute value of the background ENSO index in computing the correlation we consider the ENSO phases only and treat the cold and the warm cases as if they were the same. In Cai et al. (2003), the available time series was much longer so that the background Niño-3 index for the ZC model was composited over many cases and the results arranged evolving from the cold stage to the warm stage. This resulted in the peak of the bred vector growth rate split equally before and after the ENSO event. We can conclude that our results are qualitatively in good agreement with those obtained with the ZC model in Cai et al. (2003). The results shown here suggest that the breeding method can serve to detect the slow, coupled instability related to ENSO variability by selecting the proper rescaling parameter in the breeding cycle. Evans et al. (2004) also showed that the bred vector growth rate could be used to detect the forthcoming regime changes of the background state (from positive to negative conditions or vice versa).

b. The structure of the coupled BV mode

The spatial patterns of the ENSO coupled BV (among all the instabilities present in the system) can be identified by constructing regression maps for both oceanic and atmospheric variables against the BV Niño-3 index, defined as the spatial average of the BV SST in the Niño-3 domain. Such spatial structure of the bred vector indicates the linear response related to the ENSO instability and makes the low-frequency variations associated with ENSO clearer. We will compare the ENSO BV maps with the background ENSO regression maps constructed with the same regression method but using the background Niño-3 index. This will allow us to assess whether the coupled BV has a dominant ENSO growing component, whether it projects on the background ENSO variability, and what physical mechanisms are suggested by the BV ENSO patterns.

The oceanic global regression maps for the background fields show typical tropical variability corresponding to the ENSO mature stage (Figs. 4a-c). These patterns include a large warming extending from the east to central equatorial Pacific, a deepening thermocline in the eastern equatorial Pacific, an accompanying shoaling feature off the equator in the western basin, and a basinwide eastward current anomaly. The regression maps for the BV fields (regressed upon the BV Niño-3 index) are shown in Figs. 4d-f. The coupled BV mode exhibits a strong signal in the equatorial Pacific and fairly weak variability away from the Tropics. The patterns of the coupled BV mode are reminiscent of those in the background state except that the BV mode is more confined to the east and to the equator. This feature is physically meaningful since it reflects that the dynamical growing perturbation is mainly determined by the background structure of the thermocline. It is also consistent with the delayed oscillator theory, which considers that the perturbations grow primarily over the eastern equatorial basin through the proportionality between wind stress and the displacement of the thermocline (Cane et al. 1990). The shoaling thermocline in the east implies that the thermodynamic feedback between SST and near-surface ocean variables is much stronger in the east than in the west. As a result, oceanic perturbations in the eastern basin will be easily amplified through positive feedbacks from air-sea interaction. Although we have obtained the ENSO BV by regression with the BV Niño-3 index, Figs. 4d-f can also be referred to as the leading BV mode because they have the same structure as the leading mode obtained by applying EOF analysis to the oceanic BV (as shown in Figs. 8a,b).

The atmospheric components of the ENSO mode derived from both the background and the BV field are displayed in Fig. 5. In the same way that the background regression maps shown in Figs. 5a–d reflect the typical atmospheric response of ENSO events, the BV atmospheric regression map also exhibits the coupled feature corresponding to the boundary heating perturbation shown in Fig. 4d. Figures 5e,f show that the pat-



FIG. 4. Oceanic regression maps in the global domain: (left) the background fields and (right) the BV fields. (a) SST anomaly (°C); (b) Z_{20} anomaly (m); (c) surface zonal current anomaly (m s⁻¹); (d) BV SST (°C); (e) BV Z_{20} (m); and (f) BV surface zonal current (m s⁻¹). Background fields are regressed with the background Niño-3 index and BV fields are regressed with the BV Niño-3 index. The scales of BV fields are arbitrary, but the ratio among BV variables (both oceanic and atmospheric variables) is retained as in the original. The background Z_{20} anomaly and BV Z_{20} are only plotted within 20°N/S, since Z_{20} is defined as the depth of the 20° isotherm, so it is not well defined beyond the Tropics.

terns in the BV fields have some features in common with the patterns of the background state, such as the westerly wind perturbations located in the central equatorial Pacific and the high-low pattern in the BV surface pressure field. The baroclinic structure in the height fields corresponds to the location of BV SST in Fig. 4d. In addition, the BV outgoing radiation reflects an enhanced convection activity in the eastern basin. This atmospheric structure, implying that an amplified perturbation in the eastern Pacific induces a westerly zonal wind perturbation, indicates unstable air-sea interaction in the eastern Pacific. These features suggest that the bred perturbation is related to the coupled instability and therefore that we can refer it to as the coupled BV mode.

The NSIPP system shares a deficiency frequently

present in coupled GCMs, that is, the simulated SST variability in the eastern Pacific is smaller than the observed variability. Rienecker et al. (2000) suggest that such deficiencies may be associated with the atmospheric circulation in the tropical eastern Pacific not representing well the Walker circulation, which also limits the spread of ensemble SSTs. The high–low pressure patterns in Figs. 5f,g suggest that the coupled BV is able to reflect the impact of coupled instability upon the background atmospheric circulation by perturbing the longitudinal Walker circulation along the equator.

It is of interest to point out that the coupled BV also reflects the sensitivities in extratropical regions associated with background ENSO atmospheric teleconnections. Shown in Fig. 6 are the regression maps of surface pressure and 200-hPa geopotential in the Northern



FIG. 5. As in Fig. 3 except for the atmospheric regression maps over the equatorial Pacific basin: (a) wind field anomaly at 850 hPa $(m s^{-1})$; (b) surface pressure anomaly (hPa); (c) geopotential anomaly at 200 hPa $(m^2 s^{-2})$; (d) outgoing longwave radiation (W m⁻²); (e) BV wind field at 850 hPa $(m s^{-1})$; (f) BV surface pressure (hPa); (g) BV geopotential at 200 hPa $(m^2 s^{-2})$; and (h) BV outgoing longwave radiation (W m⁻²).

Hemisphere for the background state and for the BV field. The teleconnection patterns of the background state indicate a low pressure anomaly over the North Pacific and a high pressure anomaly over North America. This teleconnection pattern has a barotropic structure that extends from the surface to 100 hPa. It is induced by wave train patterns associated with the large-scale heating in the Tropics. Strong responses can also be identified in those regions in the BV maps, especially where background regression maps show a strong gradient, for example in the mid-Pacific at 30°N and at east coast of North America. Wave train patterns can also be found in BV regression maps. In the southern extratropical region (not shown), atmospheric regression maps also have a teleconnected pattern associated with the background ENSO, and we observe related BV dynamical sensitivities.

To show the sensitivity of the coupled BV mode to the background ENSO evolution, we construct 6-month lead/lag correlation maps against the time series of the amplitude of the background Niño-3 index (Fig. 7). In this figure, the BV fields are reconstructed using the first 10 EOF modes to illustrate the dominant signals, and significance tests are included. For the significance test, we generated surrogate BVs by randomly choosing the BV fields from original BVs so that the time dependence in the BV field is destroyed. These surrogate BV maps were regressed with the background Niño-3 index and the procedure repeated 100 times. Significance levels higher than 90% are shaded.

The result shows that the BV SST, surface height, and zonal wind stress all have a larger correlation before the mature stage of the ENSO events in the eastern Pacific. It also suggests coupled dynamics in the BV fields because of the increase of the ocean heat content and a warm SST anomaly in the eastern basin as well as the presence of westerly wind anomalies. The 2–3month lead time in Figs. 7a,b coincides with the timing of the maximum of the BV growth rate in Fig. 2. This shows that the growing dynamic instability associated with the ENSO evolution in the NSIPP CGCM is dominant in the eastern Pacific. The sensitivity of the BV with the ENSO phases and its coupled nature suggest



FIG. 6. As in Fig. 3 except for atmospheric regression maps over the Pacific portion of the Northern Hemisphere: (a) background surface pressure anomaly (hPa); (b) background geopotential anomaly at 200 hPa ($m^2 s^{-2}$); (c) BV surface pressure (hPa); and (d) BV geopotential at 200 hPa ($m^2 s^{-2}$).

its potential use for ensemble forecasting, particularly for the purpose of effectively perturbing the coupled ENSO processes in the tropical Pacific.

c. Comparison of the NSIPP and the NCEP bred vectors

Similar breeding experiments were carried out with CFS03 coupled model. The atmospheric component uses the current version of medium-range forecast (MRF) global model with a spectral truncation of 62 waves (T62) in the horizontal (equivalent to nearly 200 km) and 64 vertical levels in sigma coordinate (Kanamitsu et al. 1991; Saha et al. 2004). The ocean component is the Geophysical Fluid Dynamics Laboratory (GFDL) Modular Ocean Model V.3 (MOM3) with 40 layers in the vertical (Pacanowski and Griffies 1998). The zonal resolution is 1° and the meridional resolution is $1/3^{\circ}$ between 10°S and 10°N, gradually increasing through the Tropics until it is fixed at 1° poleward of 30°S and 30°N.

Two independent breeding experiments were performed by choosing the last 4 yr from a 23-yr perfect model experiment as the background state. This 4-yr period includes a warm event, which matures at model year 21, two years after starting the breeding run. The rescaling factor for NCEP bred perturbations is based on the SST norm computed over the whole tropical belt (10°S–10°N), not just in the tropical Pacific Niño-3 region like in the NSIPP BV. The perturbation size for the NCEP system was similar $(0.1^{\circ}C)$ and the rescaling period of one month was the same as in the breeding experiments performed with the NSIPP CGCM. Like the NSIPP coupled experiments, the two BV runs for the NCEP system were very similar despite having been started with different random perturbations so that their results are processed as a single 8-yr time series. Comparisons between the results from the NSIPP and the NCEP coupled system are now presented showing the extent to which bred vectors are sensitive to the coupled GCMs.¹

We first compare the ENSO characteristics in the background runs of the two coupled GCMs. Figures

¹ Unfortunately, the experiments performed at NCEP were erased, so we have only a limited number of diagnostic comparisons available.



FIG. 7. Lead/lag correlation maps along the equator for BV oceanic fields, reconstructed with the first 10 EOF modes, against the absolute value of the background Niño-3 index: (a) SST (°C); (b) surface height (m); and (c) zonal wind stress (N m⁻²). The light (dark) gray shading denotes the significance level higher than 90% (95%).

8a–f are the background oceanic regression maps showing that the oceanic components from both CGCMs successfully reproduce the fundamental features of ENSO. However, they also have differences reflecting differences of numerical schemes in the model dynamics or different choices of physical parameterizations. The meridional structure of warming and thickening surface height (Figs. 8d,e) in the NCEP/CFS03 GCM in the eastern Pacific is wider than that of the NSIPP GCM (Figs. 8a,b). In addition, the regressed surface height of NCEP/CFS03 shows the southern branch of the shoaling patterns off the equator extending farther southward instead of being meridionally limited as in the NSIPP case. This can also be seen in the SST and zonal current patterns.

Despite these differences in the background, the bred vectors from the two coupled systems have major similarities linked with the characteristics of the background ENSO. To compare BV structures, we show the leading EOFs of oceanic variables. Figures 9a-c are the first EOF mode of the BV SST and the first two modes for the BV thermocline from the NSIPP CGCM; Figs. 9d-f are the same modes using the BV from NCEP. Despite the fact that these are two different CGCMs with significantly different background evolution, there is a strong resemblance between the BV EOF modes. Both of the leading modes (EOF1) in NSIPP and NCEP bred vectors based on SST show an ENSOassociated warm feature in the tropical eastern Pacific farther east than in their respective background. Recalling that bred perturbations are rescaled in different regions (Niño-3 region for NSIPP and the complete tropical belt including three ocean basins for NCEP), the similarity observed in Figs. 9a and 9d indicates that the tropical Pacific dominates the growth of the BVs. However, reflecting the different mean structures and background ENSO variabilities from the two coupled systems, the NCEP BV EOF1 extends farther in space, covering the whole Niño-3 domain, while the NSIPP BV EOF1 is confined to east of 130°W and is limited in the meridional direction. The EOF1 modes representing ENSO variability explain 11% and 14% of the total variance of the growing SST perturbations in the NSIPP and NCEP models, respectively. Recall that the coupled growing perturbations include those due to a wide range of instabilities that appear in a coupled model. The fact that the leading EOF modes from BV fields in both coupled systems show a similar ENSOlike structure confirms our conjecture that the breeding method is capable of capturing the coupled instability even in the presence of other types of instabilities in the fully coupled GCM model. Moreover, this mode is robust and dominant since it is reproducible with different CGCMs and points out that the equatorial eastern Pacific is the most dynamically sensitive region for the growth of SST perturbations. Such a result indicates that the breeding method can help to identify the growing coupled instability related to the ENSO variability in a global coupled model.

Similar natural sensitivities in the eastern Pacific can also be found in the BV thermocline fields of both systems (Figs. 9b,c,e,f). For the background thermocline evolution (not shown), there are two dominant EOF modes related to the ENSO evolution: the leading one has a large variance in the eastern Pacific and the second one, representing an earlier transition, shows the anomalous deepening that starts from the subsurface of the western Pacific. We also examine the first two EOF modes for the BV thermocline. The result shows that both leading EOF thermocline modes from the two



FIG. 8. Background oceanic regression maps for two coupled GCMs in the tropical Pacific domain: (left) The NSIPP anomalies and (right) the NCEP/CFS03 anomalies. (a) NSIPP SST (°C); (b) NSIPP surface height (m); (c) NSIPP surface zonal current (m s⁻¹); (d) NCEP SST (°C); (e) NCEP surface height (m); and (f) NCEP surface zonal current (m s⁻¹). The regression maps of NSIPP (NCEP) fields are computed using the NSIPP (NCEP) Niño-3 index.

CGCMs have a deepening feature along the equator and shoaling features off the equator in the eastern basin, except that the EOF1 from NCEP extends farther across the whole basin. In addition, both EOF2 modes have a dipole pattern along the equator and establish a wave couplet off the equator in the western basin. The EOF2 emphasizes the role of the subsurface in the western-central Pacific. Examining the BV thermocline evolution off the equator, we found that the BV thermocline also has an earlier westward propagation, like the background anomalies, and that the timing of the westward propagation is linked with the background wind stress curl. These features in Fig. 9 and in the off-equator evolution suggest that the BV thermocline develops in a form of Kelvin/Rossby wave packages, propagating the upwelling/downwelling signals in the tropical region. It should be noted that the EOF1 of the BV thermocline is closely related to the EOF1 of BV SST since there is a high correlation between their corresponding leading principal components (not shown). These two modes represent the dominant growing coupled instability, which has also been obtained by the BV oceanic regression maps. The robustness of the results from two different coupled models supports our hypothesis that the leading EOFs of the bred vectors are associated with the background ENSO variability. The differences between the BVs indicate that bred vectors inherit the background characteristics associated with the model. For example, different vertical mixing schemes adopted in ocean models will have an impact on thermocline variations, particularly in the shallow mixed layer region.

Based on the regression maps against the BV Niño-3 index (not shown) in the tropical region, we can also infer that the coupling strengths are different in the two coupled GCMs. In both ocean components, a 1-m variation (deepening) in BV thermocline corresponds to 0.1°C warming in the eastern Pacific. The corre-



FIG. 9. The leading EOFs of the BV SST and Z_{20} perturbations derived from the NSIPP and NCEP/CFS03 CGCMs: (a) EOF1 of NSIPP BV SST; (b) EOF1 of NSIPP BV Z_{20} ; (c) EOF2 of NSIPP BV Z_{20} ; (d) EOF1 of NCEP BV SST; (e) EOF1 of NCEP BV Z_{20} ; and (f) EOF2 of NCEP BV Z_{20} . The scale is arbitrary.

sponding BV zonal wind stress shows a perturbation of 1.5 N m^{-2} from the NSIPP AGCM, and it prevails in the central basin. In contrast, the corresponding stress perturbation is only 0.5 N m^{-2} in the NCEP case. In addition, the regressed BV surface pressure and geopotential height for the NCEP model are less organized in the Tropics than for the NSIPP coupled model. This seems to suggest that tropical perturbations are more strongly coupled in the NSIPP CGCM than in the NCEP CGCM.

The similarity between the two systems can also be identified in the extratropical ENSO-associated teleconnection. Figures 10a,b are the regression maps of BV geopotential height at 500 hPa from the two coupled models. Similar responses can be found from the northeastern Pacific to the North Atlantic despite the different responses for other locations. These teleconnected regions are largely constrained by the variations of the tropical heating. The resemblance for bred vectors in these locations suggests that the bred vector could be an "effective" ensemble ENSO perturbation in the sense that it projects the perturbation growth onto areas in the global atmosphere associated with ENSO variability.

Additional experiments with the NCEP/CFS03 CGCM have confirmed that the relationship between the BV growth rate and the phase of ENSO events remains similar with a rescaling period of 15-day rather than the one month used so far (M. Peña 2005, personal communication).

4. Summary and discussion

In this study, we demonstrated, for the first time, the feasibility of applying the breeding method to a global coupled ocean–atmosphere general circulation model to obtain ENSO coupled instabilities. The characteristics of the coupled bred vector have been first examined



(a) NSIPP regressed BV geopotential height at 500hpa

FIG. 10. Atmospheric regression maps in the Northern Hemisphere of BV sea level pressure (hPa) (a) for NSIPP and (b) for NCEP/CFS03. Both fields are computed against their own BV Niño-3 indices.

120E

180

120W

in the NSIPP coupled model under a perfect model scenario.

60E

EQ 105

The results show that the breeding method can obtain the growing coupled modes associated with ENSO variability and that the BV growth rate is sensitive to the background ENSO evolution, with the maximum leading the warm/cold events by three months. This lead time in our results (compared with 6-12 months for the ZC model) may seem to be too short for improving the current ensemble forecast system. However, we believe that this relatively short lead time is partially due to the fact that the ENSO cycle in this long simulation is more biennial than 3-7 years. The biennial time scale shortens the "growing season" of bred vectors because of the relatively fast pace of the evolving background state. We would expect to obtain a longer lead time from a BV growth rate derived from the NSIPP operational system since it will reflect the real oceanic memory from the observations during initialization, although the shorter time lag may be also associated with the presence of other weather and oceanic instabilities. We have explored this question with the current NSIPP operational system, which includes real ocean observations, and where we used as background the updated analysis fields. Preliminary results

indicate that the lead time is lengthened by about 2 months.

60%

One of the main tasks in our study has been to extract the physical growing mode from the total growth variability, separating the ENSO signal from noise associated with weather and other less relevant instabilities. We used regression BV maps to illustrate that the ENSO-associated features can be captured by the breeding method. For the oceanic fields, the variability mainly comes from the tropical eastern Pacific, where the background anomalies have large variance due to the mean structure of the thermocline. We also show that the atmospheric BV in the Tropics carries the coupled features reflecting the growing perturbations at the boundary due to the unstable air-sea interaction. Such structure exhibits a longitudinal Walker-like circulation along the equator. Evidence from the lead/lag correlation maps suggests that such growing perturbation is related to the background ENSO variability. In addition to the coupled characteristics shown in the tropical domain, the extratropical circulation anomalies associated with the coupled BV display a wave-train teleconnection pattern over the North Pacific and North America, areas known to be strongly teleconnected to ENSO variability.

The robustness of the coupled BV modes has been demonstrated by comparing bred vectors derived from the NSIPP CGCM and NCEP/CFS03 CGCMs. The two coupled GCMs can both represent the main features of the ENSO events, but differences exist in the detailed structure. Our results indicate that the coupled BV structure can be reproduced by the different CGCMs, indicating very similar structure in their leading EOF modes. In addition, the differences between the leading EOF modes obtained from the two systems reflect that they inherit the characteristics of the CGCMs. Strong resemblance between these two independent experiments can be found in many fields, even in those atmospheric teleconnected regions associated with background ENSO development. Our results suggest that by selecting physically meaningful breeding parameters, one can use the breeding method to isolate the slowly varying, coupled instabilities from the fastgrowing weather signals in a coupled GCM. The global sensitivities associated with the coupled instability initiated from the tropical Pacific can be retained even though the rescaling is simply done in the tropical Pacific.

Using the same NSIPP CGCM, Kleeman et al. (2003) calculated a climate-relevant leading singular vector by using a tangent linear propagator derived from the subspace spanned by five dominant correlation EOF modes of the background SST anomaly. In their work, they focused on the SST perturbation, so we can only compare the SST structure from the two methods. Their initial singular vector shows a large warming perturbation in the tropical Pacific with a maximum located in the central Pacific. Their final singular vector after six months is very similar to our ocean regression map (Fig. 3d) with a strong amplitude in the eastern Pacific representing the mature state of ENSO. We do not have a warming feature in the northwest of the Pacific off the equator that appears in the initial singular vector. In addition, there is no clear evidence showing that the singular vector is sensitive to the ENSO phases even though the growth rates from both methods show dependence on ENSO evolution. The similarity between the bred vector and the final singular vector (but not the initial singular vector) is also characteristic of the results obtained with the ZC model (Cai et al. 2003; Xue et al. 1997b).

Our results indicate that the coupled BVs could be used in ensemble forecasting as initial perturbations that effectively project on the ENSO-related large-scale features. Therefore, the next stage of our research is to employ these methods in the NSIPP operational system. In particular, we plan to test whether ensemble forecasts with coupled BVs as initial perturbations are more effective than current ensembles using uncoupled perturbations introduced into the atmosphere or the ocean model components.

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